For #1 – 18: Simplify the expression. Write your answer using exponents (evaluate numerical bases with powers  $\leq 4$ ).

1) 
$$x^2 \cdot x^5$$

2) 
$$y^3 \cdot y^3 \cdot y$$

3) 
$$(-5)^3 \cdot (-5)$$
 4)  $(-8)^2$ 

4) 
$$(-8)^2$$

5) 
$$-8^2$$

**6**) 
$$(2x)^3$$

7) 
$$(2x^2y^3)^5$$

8) 
$$(a^4)^8$$

9) 
$$8^5 \cdot 8^2$$

**10**) 
$$(-6)^6(-6)$$
 **11**)  $2^4 \cdot 2^9 \cdot 2$ 

11) 
$$2^4 \cdot 2^9 \cdot 2$$

12) 
$$(7^4)^3$$

13) 
$$y^9 \cdot y$$

14) 
$$(y^4)^6$$

15) 
$$-(5x)^2$$

**16**) 
$$(-8m^4)^2 \cdot m^3$$

17) 
$$(-3c^8)(2c^6d^8)$$

**18**) 
$$(2y^5)^3(2y^2)^4$$

## **Multiple Choice:**

**19**) Which expression is equivalent to  $(-9)^6$ ?

a) 
$$(-9)^2(-9)^3$$
 b)  $(-9)(-9)^5$  c)  $[(-9)^4]^2$  d)  $[(-9)^3]^3$ 

b) 
$$(-9)(-9)^5$$

c) 
$$[(-9)^4]^2$$

d) 
$$[(-9)^3]^3$$

**20)** Which expression is equivalent to  $36x^{12}$ ?

a) 
$$(6x^3)^4$$

b) 
$$12x^4 \cdot 3x^3$$

a) 
$$(6x^3)^4$$
 b)  $12x^4 \cdot 3x^3$  c)  $3x^3 \cdot (4x^3)^3$  d.)  $(6x^5)^2 \cdot x^2$ 

d.) 
$$(6x^5)^2 \cdot x^2$$

## For #21 - 24, Find the missing exponent.

**21**) 
$$x^4 \cdot x^? = x^5$$

**22**) 
$$(y^8)^? = y^{16}$$

**23**) 
$$(2z^?)^3 = 8z^{15}$$

**24**) 
$$(3a^3)^2 \cdot 2a^3 = 18a^9$$

**25**) Solve for *y*: 
$$\frac{y}{10} = \frac{7}{5}$$

**26) BONUS:** Simplify: 
$$(-2x^3y^5)^3 \cdot (5xy^4)^2$$

For #1-16, Simplify the expression. Write your answer using exponents (evaluate numerical bases with powers  $\leq 4$ ).

1) 
$$\frac{3^9}{3^5}$$

2) 
$$\frac{y^{15}}{y^9}$$

3) 
$$\frac{6^7 \cdot 6^4}{6^6}$$

4) 
$$\frac{9^8}{9^6}$$

$$5) \ \frac{a^4}{a}$$

$$6) \left(\frac{-1}{x}\right)^3$$

7) 
$$(x^3y)^4$$

8) 
$$\left(\frac{2}{b^2}\right)^3$$

$$9) \left(\frac{y^5}{y^2}\right)^9$$

$$10) \ \frac{x^5 y^4}{x^2 y^8}$$

11) 
$$\frac{(-4)^9}{(-4)^2}$$

$$12) \left(\frac{j}{k}\right)^{11}$$

13) 
$$\left(\frac{-4}{x}\right)^2$$

**14**) 
$$\left(\frac{7}{8}\right)^2$$

$$15) \left(\frac{a^8}{ba^3}\right)^5$$

$$16) \left(\frac{-5}{2}\right)^3$$

For #17 – 18: Find the missing exponent.

$$17) \; \frac{7^{?} \cdot 7^{2}}{7^{4}} = 7^{6}$$

$$18) \left(\frac{2c^3}{d^2}\right)^? = \frac{16c^{12}}{d^8}$$

Evaluate the expression for the given variable.

**19**) 
$$x^3$$
 when  $x = \frac{3}{4}$ 

For #20 - 21: Solve for x.

$$20) \ \frac{x+3}{4} = \frac{7x-1}{2}$$

$$21) \ \frac{10}{z-1} = \frac{12}{z+7}$$

For #22-29, simplify the expression. Write your answer using positive exponents (evaluate numerical bases with powers  $\leq 4$ ).

**23**) 
$$5(7x^3)^0$$

**24**) 
$$(-4)^0$$

25) 
$$x^{-2}$$

26) 
$$\frac{1}{6^{-2}}$$

**27**) 
$$\frac{a^5}{a^{-7}}$$

28) 
$$\frac{b^{-2}}{b^{11}}$$

$$29) \ \frac{a^3 y^3}{a^{10} y^{-5}}$$

**30) Bonus:** 
$$\frac{4b^{-14}d^2}{2^3b^{-5}d^{-7}}$$

## Algebra 1 Worksheet 6.1

For #1 - 13, solve each exponential equation.

1. 
$$2^x = 16$$

**2.** 
$$3^x = 9$$

3. 
$$4^x = 64$$

**4.** 
$$125 = 5^x$$

5. 
$$32 = 2^x$$

6. 
$$2^{2x+5} = 2^7$$

7. 
$$6^{3x-4} = 36$$

8. 
$$5^{3x-12} = 125$$

9. 
$$\frac{1}{4}(4)^x = 16$$

**10.** 
$$4\left(\frac{1}{2}\right)^x = \frac{1}{4}$$

**11.** 
$$36^{2x-7} = 6^{x-5}$$

12. 
$$36^{\frac{4}{3}\chi} = 6^8$$

**13**. 
$$5^{3x-5} + 10 = 635$$

Simplify each expression using exponential rules (note: don't leave negative exponents in final answer). 14.  $(-6m^5)^3 \cdot m^9$  15.  $6(8x^4)^0$ 

14. 
$$(-6m^5)^3 \cdot m^5$$

**15.** 
$$6(8x^4)^{0}$$

**16.** 
$$\left(-\frac{5}{x^4}\right)^3$$

17. 
$$\frac{a^4b^{-3}}{a^{-8}b^{12}}$$

Solve for the variable.

18. 
$$\frac{x+3}{5} = \frac{x-2}{4}$$

19. 
$$\frac{x+4}{6} = \frac{x-2}{3}$$

#20 & 21: BONUS. Show your work to receive credit

**20.** 
$$8^{4x-5} + 5 = 37$$

**21.** 
$$4^{x-8} \cdot 16 = 2^{4x-12}$$

For #1 - 5, classify each function as linear or exponential.

1.

X	-2	-1	0	1	2
y	1	2	4	8	16

2.

X	-2	-1	0	1	2
y	$\frac{1}{25}$	$\frac{1}{5}$	1	5	25

**3.** 

х	-2	-1	0	1	2
у	16	19	22	25	28

**4.** 
$$y = 3 \cdot (2)^x$$
 **5.**  $y = -6x + 9$ 

For #6-9, identify whether the exponential function models growth or decay.

**6.** 
$$f(x) = 2(4)^x$$

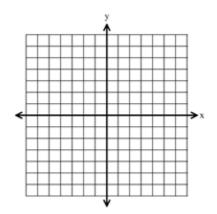
7. 
$$y = \left(\frac{1}{3}\right)^x + 2$$

8. 
$$y = (1.5)^x$$

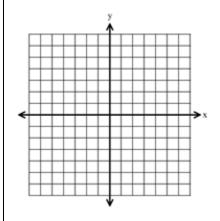
**9.** 
$$y = 3\left(\frac{2}{5}\right)^x$$

For #10 – 15, graph each exponential function. State the domain, range, and write the equation of the horizontal asymptote (H.A). A table is provided if you wish to use it.

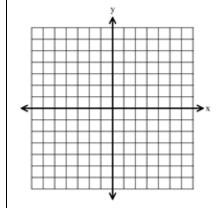
**10.**  $y = 3^x$ 



11.  $f(x) = 5^{x-2}$ 



12.  $y = \left(\frac{1}{2}\right)^{x+5} - 2$ 



Growth or Decay?

Domain: Range:

H.A:

**Transformations:** 

y

Growth or Decay?

Domain: Range:

H.A:

**Transformations:** 

X	y

Growth or Decay?

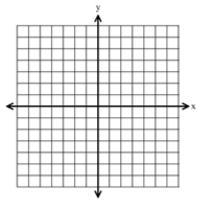
Domain: Range:

H.A:

**Transformations:** 

X	y

13. 
$$g(x) = 2^x + 1$$



Growth or Decay?

Domain:

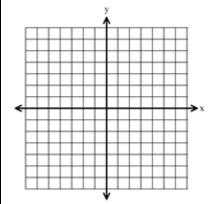
Range:

H.A:

**Transformations:** 

X	y

**14.** 
$$y = \left(\frac{1}{3}\right)^x - 3$$



Growth or Decay?

Domain:

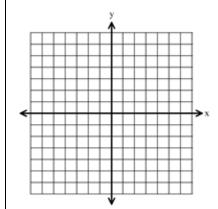
Range:

H.A:

**Transformations:** 

X	y

**15.** 
$$y = \left(\frac{1}{4}\right)^{x+5}$$



Growth or Decay?

Domain:

Range:

H.A:

Transformations:

X	y

For #16 – 17, solve for x. 16.  $3^{2x+3} = 27$ 

**16.** 
$$3^{2x+3} = 27$$

17. 
$$8^x - 20 = 44$$

For #18 - 19, solve the system using substitution or elimination.

**18.** 
$$\begin{cases} -3x - 8y = 20 \\ y = 19 + 5x \end{cases}$$

**19.** 
$$\begin{cases} x - 3y = -3 \\ -7x + 8y = -5 \end{cases}$$

For #1 - 3, state all transformations of the function and whether it is growth or decay.

1) 
$$y = 4\left(\frac{1}{2}\right)^x + 2$$

Transformations:

Growth or Decay?

2) 
$$y = 2 \cdot 3^x + 3$$

**Transformations:** 

Growth or Decay?

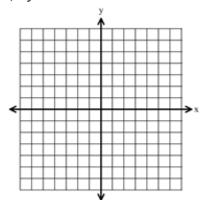
3) 
$$y = \left(\frac{1}{4}\right)^{x-1} - 2$$

Transformations:

Growth or Decay?

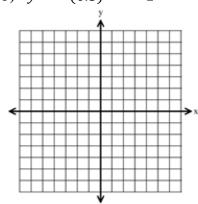
For #4-9, Graph the following functions. Identify D, R, equation of horizontal asymptote (HA), transformations, and whether it is growth or decay.

4) 
$$y = 3^{x-1} + 3$$



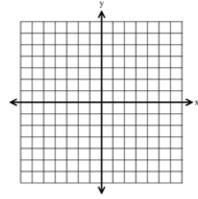
Transformations:

 $5) \quad y = -(0.5)^{x+3} - 1$ 



**Transformations:** 

6)  $y = 3 \cdot 2^{x-4} - 5$ 



**Transformations:** 

Domain: Range:

H.A: Growth/Decay?

Domain:

Range:

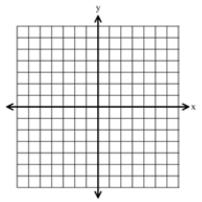
H.A: Growth/Decay?

Domain:

Range:

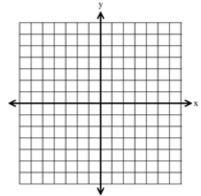
H.A: Growth/Decay?

7)  $y = \left(\frac{2}{3}\right)^{x+5} - 1$ 



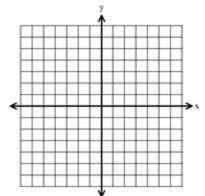
**Transformations:** 

**8**)  $y = -\left(\frac{3}{4}\right)^{x-1} + 6$ 



**Transformations:** 

9)  $y = 4 \cdot 3^{x+1} - 2$ 



**Transformations:** 

Domain: Range:

H.A: Growth/Decay?

Domain:

Range:

H.A:

Growth/Decay?

Domain:

Range:

H.A:

Growth/Decay?

10) How does the graph of  $f(x) = 3^{x+2}$  compare to the graph of  $g(x) = 3^x + 2$ ?

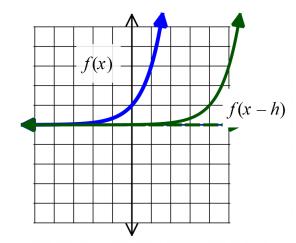
For #11 - 13, simplify using the rules of exponents.

11) 
$$(x^4)^8$$

$$12) \ \frac{x^{-4}y^3z^{-6}}{x^8y^{-2}}$$

13) 
$$x \cdot x^5 \cdot x^7$$

- **14**) Describe how  $g(x) = 2^x$  changes after the transformation -3g(x) is applied.
- 15) Given f(x) and f(x h) as graphed, find the value of h.



For problems #1-6, determine whether the function is exponential. If it is exponential, write an equation for the function in the form  $y = a_0 \cdot (b)^x$ 

1)	x	0	1	2	3
	ν	2	8	32	128

**2**) 20, 40, 80, ...

<b>4</b> )	х	0	1	2	3
	у	3	9	27	81

7) Write an equation for the exponential function below and find the 7<sup>th</sup> term.

х	0	1	2	3
у	32	16	8	4

8) Your parents offer you two options to receive an allowance for a 9-week period.

Option 1: You get paid \$25 per week

Option 2: You are paid \$1 the first week, \$2 the second week, \$4 the third week, and so on.

a) Does either option form a geometric sequence? Explain.

**b)** If you want to receive the most possible money in the 9 week period, which option should you choose? Explain.

For #9 - 11, write the recursive formula for each geometric sequence.

11) 
$$\frac{1}{2}$$
,  $\frac{3}{10}$ ,  $\frac{9}{50}$ ,  $\frac{27}{250}$ , ...

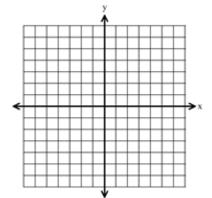
For #12 – 13, simplify each expression using exponent rules.

$$12) \quad \left(-\frac{4}{x^5}\right)^8$$

$$13) \quad \frac{b^{12}c^{-4}}{b^{-3}c^{-2}}$$

For #14-15, Graph the following exponential functions including the horizontal asymptote (HA). Identify D, R, equation of asymptote, transformations, and growth/decay.

**14**) Graph  $y = 4^{x-2} + 3$ 



**Transformations:** 

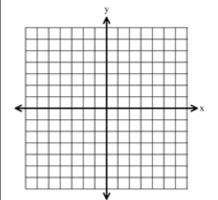
Domain:

Range:

H.A:

Growth/Decay?

**15**) Graph  $y = \left(\frac{1}{4}\right)^{x+3} - 2$ 



Transformations:

Domain: Range:

H.A:

Growth/Decay?

**16**) Describe how  $g(x) = 5^x$  changes after the transformation g(x) + 4 is applied.

For #17-18, solve the system using elimination. Show all your work.

$$17) \begin{cases} 16x - 10y = 10 \\ -8x - 6y = 6 \end{cases}$$

18) 
$$\begin{cases} -7x - 8y = 9 \\ -4x + 9y = -22 \end{cases}$$

**Bonus:** Solve for *x*. Show your work.

$$49^{3x+8} = 7^{x+6}$$

For #1-6, Given the exponential function, identify the initial amount a and the growth/decay factor b.

1. 
$$y = 25(1.20)^x$$

**2.** 
$$f(x) = 1250(.65)^x$$

3. 
$$y = 1.17^x$$

Initial amount:

Initial amount:

Initial amount:

Growth/decay factor:

Growth/decay factor:

Growth/decay factor:

**4**. 
$$y = 2(.83)^x$$

**5.** 
$$f(t) = .678 \cdot (1.9)^t$$

**6.** 
$$y = .97^x$$

Initial amount:

Initial amount:

Initial amount:

Growth/decay factor:

Growth/decay factor:

Growth/decay factor:

For #7-9, identify if the function is a growth or decay function.

7. 
$$f(t) = -2.3 \cdot 5^t$$

**8.** 
$$f(x) = .15(2)^{-x}$$

**9.** 
$$y = -3\left(\frac{1}{6}\right)^{-x}$$

- **10.** You are given a gift of \$2,500 in stock on your 16<sup>th</sup> birthday. The value of the stock declines by 10% per year.
  - **a)** Write an exponential decay function that could be used to find the value of the stock t-years after your 16<sup>th</sup> birthday.
  - **b**) What will the value of the stock be on your 21<sup>st</sup> birthday? Round to the nearest cent. (use a calculator)
- 11. Samantha buys a house for \$125,000. The value of the house increases by 3% each year.
  - **a)** Write an exponential growth function to model the value of Samantha's house t-years after she bought it.
  - **b)** What is the value of Samantha's house 7 years after she purchased the house? Round to the nearest cent. (use a calculator)
- **12.** You deposit \$500 into a savings account that earns 6% interest each year and you do not make any deposits or withdrawals. How much will the account be worth in 25 years?

- 13. Jimmy buys a car for \$15,000. The value of the car depreciates by 7% each year.
  - a) Write an exponential decay function to model the value of Jimmy's car t-years after he bought it.
  - **b)** What is the value of Jimmy's car 4 years after he purchased the car? Round to the nearest cent. (use a calculator)

For #14 - 15, simplify each expression using the rules of exponents.

**14.** 
$$(-3a^2b)^2 \cdot 6a^5b^4$$

15. 
$$\left(\frac{3y^8}{x^2y^3}\right)^2$$

For #16 - 17, solve for the variable.

**16.** 
$$3^{5x-11} + 9 = 90$$

17. 
$$\frac{1}{3}(6)^x = 72$$

**18.** Graph: 
$$y = 5^{x+3} + 3$$

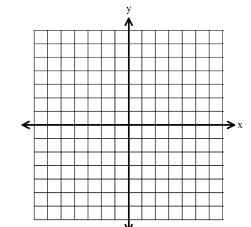
Growth/Decay?

Domain:

Range:

H.A:

Transformations:



## **Algebra 1 Chapter 6 Practice Test**

Name \_\_\_\_\_\_ Per \_\_\_\_

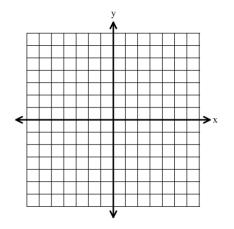
For #1-4, Graph the Exponential function.

1) 
$$y = -3^{x+1} - 5$$

Domain: Range:

Transformations:

Growth/Decay?



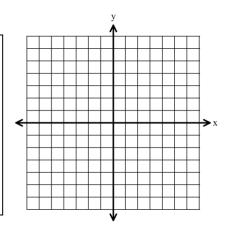
2) 
$$y = \left(\frac{1}{2}\right)^{x-3} + 2$$

Domain:

Range:

Transformations:

Growth/Decay?



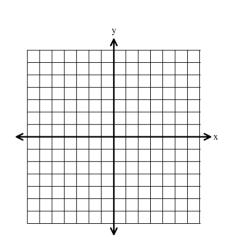
3) 
$$y = 4 \cdot 2^x + 1$$

Domain:

Range:

Transformations:

Growth/Decay?



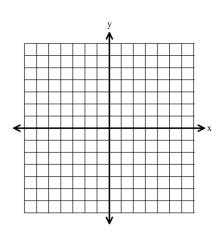
4) 
$$y = 2 \cdot (3)^{x-4}$$

Domain:

Range:

Transformations:

Growth/Decay?



For #5 - 8, Write an equation for the exponential functions.

X	0	1	2	3
y	$-\frac{1}{16}$	$-\frac{1}{4}$	-1	-4

X	0	1	2	3
y	25	5	1	$\frac{1}{5}$

8) 
$$\frac{7}{2}$$
, 14, 56, ...

For #9 –	<b>10:</b> Sam buys	a car for \$55,0	00. The va	lue of the c	ar depreciates	at a rate of	12% per ye	ar. Use a
calculato	r when needed							

- 9) Write an exponential equation to model the situation.
- 10) What will the value of the car be 4 years after Sam purchases the car?

For #11 - 12: Dan buys a rare car at auction for \$35,000. The value of the car increases by 12.5% per year. Use a calculator when needed.

- 11) Write an exponential equation to model the situation.
- 12) What will the value of the car be 5 years after Dan purchases the car?

For #13 – 14: 
$$g(x) = 900(.65)^x$$

- 13) Does the function g(x) represent exponential growth or decay?
- 14) What is the growth **factor** or decay **factor** for g(x)?

For #15 – 17: 
$$f(x) = 657(1.42)^x$$

- 15) Does the function f(x) represent exponential growth or decay?
- 16) What is the growth **factor** or decay **factor** for f(x)?
- 17) What is the initial amount for f(x)?

For problems #18 - 23, solve the equation.

18) 
$$4^x = 64$$

19) 
$$9^x = 81$$

20) 
$$7^{3x} = 7^{x+8}$$

$$21) \ \frac{1}{4}(4)^x = 4$$

22) 
$$49^{3x} = 7^{4x+8}$$

23) 
$$6^{3x-1} = 36^{3x-5}$$

For problems #24 - 27, simplify using the rules of exponents.

24) 
$$(y^8)^5$$

25) 
$$x^3 \cdot x^4 \cdot x^6$$

$$26) \ \frac{x^{-2}y^5z^{-2}}{x^8y^{-2}z^{-6}}$$

27) 
$$(2x^5y^4)^3 \cdot 2xy$$